## SUPPLEMETARY MATERIALS

# Brain blood flow pulse analysis may help to recognize individuals who suffer from hydrocephalus 

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## Distorted pulses removing

Based on the visual inspection of all detected pulses, the following criteria were applied to the algorithm written in Python for the automatic removal of distorted pulses: 1) pulse shorter than 0.33 s or longer than 1.5 s (outside the physiological range of pulse length), 2) appearance time of the maximum CBFV pulse greater than 0.35 s (the maximum associated with a first or second peak of the CBFV pulse should appear within 0.3 s from the beginning of the pulse [1]), 3) the last
sample of a detrended and normalized $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse greater than 0.15 (the minimum value of the detrended $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse is expected at the end of the pulse, otherwise the pulse is detected incorrectly), 4) maximum triangle distance between triangle and $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse curve greater than 0.65 (high amplitude of $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ oscillation are not expected in the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse, based on the shape of the pulse observed in MRI studies [2]).

## $\mathrm{Ca}_{\mathrm{a}} \mathrm{BV}$ calculation

To calculate $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulses from the non-invasively measured CBFV signal the constant flow forward model of cerebral blood circulation was applied [3]. The main assumptions of this model are that: 1) cerebral blood outflow $\left(\mathrm{CBF}_{\text {out }}\right)$ is significantly less pulsatile than cerebral blood inflow $\left(\mathrm{CBF}_{\text {in }}\right)[4]$ and therefore $\mathrm{CBF}_{\text {out }}$ can be approximated by the mean value of $\mathrm{CBF}_{\text {in }}$ over a 6 seconds window [3] (see Supplement Figure 1a); 2) cerebral blood inflow can be estimated with CBFV multiplied by cross-sectional area of insonated artery (see equations in Supplement Figure 1a,b).


Supplement Figure 1. a): visualization of cerebral blood volume (CBV) calculated over a single cardiac cycle using invasively measured cerebral blood inflow and cerebral blood outflow (based on [4]). b): visualization of non-invasively estimated cerebral arterial blood volume ( $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ ) using constant flow forward model and TCD cerebral blood flow velocity signal. For the description of the assumptions see the content of Supplementary material. $t_{0}$ - beginning of a cardiac cycle, $S_{a}$ - cross-sectional area of the insonated artery.

It was also assumed that the cross-sectional area of the insonated artery remains constant over a series of cardiac cycles [4], [5]. With these assumptions, the cross-sectional area of the insonated artery can be neglected in the equation in Figure 1b), and changes in $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ can be estimated using Equation (1).

$$
\begin{equation*}
\Delta C_{a} B V(t)=\int_{t_{0}}^{t}(C B F V(x)-\operatorname{mean}(C B F V)) d x[\mathrm{~cm}] \tag{1}
\end{equation*}
$$

where $\Delta \mathrm{C}_{\mathrm{a}} \mathrm{BV}$ is the change in cerebral arterial blood volume during a single cardiac cycle, $\mathrm{t}_{0}$ is the beginning of a single cardiac cycle, $\operatorname{CBFV}(\mathrm{x})$ is cerebral blood flow velocity at the moment t $[\mathrm{cm} / \mathrm{s}]$, mean $(\mathrm{CBFV})$ is a mean cerebral blood flow velocity calculated over a 6 seconds window [ $\mathrm{cm} / \mathrm{s}]$.

It is important to note that $\Delta \mathrm{C}_{\mathrm{a}} \mathrm{BV}$ calculated in this way is normalized (divided) by the unknown cross-sectional area of the vessel $\mathrm{S}_{\mathrm{a}}$; therefore, units are not units of volume $\left(\mathrm{cm}^{3}\right)$ but cm and the value of $\Delta \mathrm{C}_{\mathrm{a}} \mathrm{BV}$ cannot be compared between subjects. This however does not affect the shape of the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse, making the comparison analysis of the pulse shapes between healthy volunteers and NPH patients possible.

Supplement Table 1. List of all triangle similarity parameters that were analyzed.

| Parameter name | Acronym | Parameter name | Acronym |
| :--- | :--- | :--- | :--- |
| Total Area - sum of all areas <br> where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is <br> above or below the triangle arm <br> on both ascending and <br> descending parts of the pulse | TA | mean Ascending Lower Distance <br> - the average distance calculated <br> from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour <br> is below the triangle on ascending <br> part of the pulse | mALD |
| mean Distance - the average <br> distance calculated from all <br> areas between $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse <br> contour and triangle arms | mD | Maximum Ascending Lower <br> Distance - the maximum distance <br> calculated from area where the | MALD |


| Maximum Distance - the maximum distance from all areas between $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour and triangle arms | MD | Descending Upper Area - the area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is above the triangle on descending part of the pulse | DUA |
| :---: | :---: | :---: | :---: |
| Upper Area - sum of areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is above the triangle arms | UA | mean Descending Upper <br> Distance - the average distance calculated from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is above the triangle on descending part of the pulse | mDUD |
| mean Upper Distance - the averaged distance calculated from all areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is above the triangle arms | mUD | Maximum Descending Upper Distance - the maximum distance calculated from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is above the triangle on descending part of the pulse | MDUD |
| Maximum Upper Distance the maximum distance from all areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is above the triangle arms | MUD | Descending Lower Area - the area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is below the triangle on descending part of the pulse | DLA |
| Lower Area - sum of areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is below the triangle arms | LA | mean Descending Lower <br> Distance - the average distance calculated from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is below the triangle on descending part of the pulse | mDLD |
| mean Lower Distance - the averaged distance calculated from all areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is below the triangle arms | mLD | Maximum Descending Lower Distance - the maximum distance calculated from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is below the triangle on descending part of the pulse | MDLD |
| Maximum Lower Distance the maximum distance from all areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is below the triangle arms | MLD | Ascending Descending Duration Ratio - the ratio of the duration of the ascending and descending part of the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse | ADDR |
| Lower Upper Area Ratio - the ratio of the sum of the areas where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse is above the arms of the triangle to the sum of the areas where the | LUAR | Frechet Distance - distance between $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour and the triangle arms calculated with the use of frechetdist 0.6 Python package, based on [6] | FD |

$\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour is below the arms of the triangle.

Ascending Upper Area - the area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is above the triangle on ascending part of the pulse
mean Ascending Upper
Distance - the average distance calculated from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is above the triangle on ascending part of the pulse
Maximum Ascending Upper
Distance - the maximum distance calculated from area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is above the triangle on ascending part of the pulse
Ascending Lower Area - the area where the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ contour is below the triangle on ascending part of the pulse

Dynamic Time Wrapping
Distance - distance between $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$
pulse contour and the triangle arms DTWD calculated with the use of dtwpython 1.3.0 package, based on [7]
normalized Dynamic Time Wrapping Distance - normalized distance between $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse contour and the triangle arms calculated with the use of dtwpython 1.3.0 package, based on [7]

## Maximum Appearance Time -

 the time of appearance of the MAT maximum value of the $C_{a} B V$ pulsenDTWD

| MAUD | Maximum Appearance Time - <br> the time of appearance of the <br> maximum value of the $\mathrm{C}_{\mathrm{a}} \mathrm{BV}$ pulse | MAT |
| :--- | :--- | :--- |

mAUD

Supplement Table 2. Medians, lower (Q1) and upper (Q3) quartiles of all triangle similarity parameters. P-values are from the Wilcoxon signed rank test. Medians and p-values above 0.05 are bolded. Parameter names are given as acronyms, see Table 1 for full names.

## Healthy volunteers $\mathbf{n}=\mathbf{2 3} \quad$ NPH patients $\mathbf{n}=\mathbf{3 1}$

| Parameter | Median | Q1 | Q3 | Median | Q1 | Q3 | p-value |
| :--- | ---: | :--- | :--- | ---: | :--- | :--- | ---: |
| TA | $\mathbf{2 6 . 4 5}$ | 23.56 | 27.81 | $\mathbf{2 2 . 4 7}$ | 21.42 | 27.21 | $\mathbf{0 . 0 2 5}$ |
| mD | $\mathbf{0 . 1 3 2}$ | 0.118 | 0.139 | $\mathbf{0 . 1 1 2}$ | 0.107 | 0.136 | $\mathbf{0 . 0 2 5}$ |
| MD | $\mathbf{0 . 2 9 0}$ | 0.251 | 0.310 | $\mathbf{0 . 2 5 3}$ | 0.215 | 0.293 | $\mathbf{0 . 0 1 7}$ |
| UA | $\mathbf{2 6 . 1 3}$ | 23.19 | 27.57 | $\mathbf{2 1 . 8 2}$ | 20.54 | 27.08 | $\mathbf{0 . 0 1 7}$ |
| mUD | $\mathbf{0 . 1 4 4}$ | 0.129 | 0.150 | $\mathbf{0 . 1 3 0}$ | 0.122 | 0.145 | $\mathbf{0 . 0 2 4}$ |
| MUD | $\mathbf{0 . 2 8 9}$ | 0.251 | 0.308 | $\mathbf{0 . 2 5 3}$ | 0.215 | 0.293 | $\mathbf{0 . 0 1 7}$ |
| LA | $\mathbf{0 . 3 7 4}$ | 0.265 | 0.497 | $\mathbf{0 . 6 6 1}$ | 0.344 | 1.296 | $\mathbf{0 . 0 0 5}$ |
| mLD | $\mathbf{0 . 0 1 7}$ | 0.014 | 0.021 | $\mathbf{0 . 0 2 6}$ | 0.019 | 0.032 | $\mathbf{0 . 0 0 2}$ |
| MLD | $\mathbf{0 . 0 3 3}$ | 0.027 | 0.041 | $\mathbf{0 . 0 5 0}$ | 0.036 | 0.059 | $\mathbf{0 . 0 0 3}$ |
| LUAR | $\mathbf{0 . 0 1 7}$ | 0.008 | 0.030 | $\mathbf{0 . 0 3 1}$ | 0.016 | 0.061 | $\mathbf{0 . 0 4 8}$ |


| AUA | $\mathbf{1 0 . 4 7}$ | 9.775 | 14.16 | $\mathbf{6 . 7 6 0}$ | 5.497 | 8.870 | $\ll \mathbf{0 . 0 0 1}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: |
| mAUD | $\mathbf{0 . 1 5 3}$ | 0.141 | 0.170 | $\mathbf{0 . 1 1 4}$ | 0.097 | 0.130 | $\ll \mathbf{0 . 0 0 1}$ |
| MAUD | $\mathbf{0 . 2 5 8}$ | 0.237 | 0.296 | $\mathbf{0 . 1 8 3}$ | 0.152 | 0.239 | $\ll \mathbf{0 . 0 0 1}$ |
| ALA | $\mathbf{0 . 3 1 4}$ | 0.200 | 0.452 | $\mathbf{0 . 5 9 9}$ | 0.322 | 1.241 | $\mathbf{0 . 0 0 2}$ |
| mALD | $\mathbf{0 . 0 2 1}$ | 0.017 | 0.025 | $\mathbf{0 . 0 3 1}$ | 0.023 | 0.038 | $\mathbf{0 . 0 0 3}$ |
| MALD | $\mathbf{0 . 0 3 3}$ | 0.026 | 0.040 | $\mathbf{0 . 0 4 9}$ | 0.035 | 0.059 | $\mathbf{0 . 0 0 2}$ |
| DUA | $\mathbf{1 3 . 4 8}$ | 12.91 | 15.08 | $\mathbf{1 5 . 0 4}$ | 12.96 | 17.21 | 0.157 |
| mDUD | $\mathbf{0 . 1 2 8}$ | 0.119 | 0.135 | $\mathbf{0 . 1 3 1}$ | 0.119 | 0.143 | 0.421 |
| MUDD | $\mathbf{0 . 1 9 8}$ | 0.187 | 0.213 | $\mathbf{0 . 2 1 4}$ | 0.186 | 0.230 | 0.151 |
| DLA | $\mathbf{0 . 0 4 3}$ | 0.036 | 0.060 | $\mathbf{0 . 0 4 6}$ | 0.020 | 0.103 | 0.958 |
| mDLD | $\mathbf{0 . 0 0 5}$ | 0.004 | 0.005 | $\mathbf{0 . 0 0 4}$ | 0.003 | 0.007 | 0.875 |
| MDLD | $\mathbf{0 . 0 0 8}$ | 0.006 | 0.009 | $\mathbf{0 . 0 0 7}$ | 0.004 | 0.011 | 0.875 |
| ADDR | $\mathbf{0 . 8 0 2}$ | 0.707 | 0.915 | $\mathbf{0 . 6 8 8}$ | 0.623 | 0.794 | $\mathbf{0 . 0 0 2}$ |
| FD | $\mathbf{0 . 1 2 1}$ | 0.110 | 0.140 | $\mathbf{0 . 1 2 7}$ | 0.104 | 0.155 | 0.916 |
| DTWD | $\mathbf{1 . 2 7 7}$ | 1.227 | 1.341 | $\mathbf{1 . 2 4 4}$ | 1.211 | 1.443 | 0.441 |
| nDTWD | $\mathbf{0 . 0 0 3}$ | 0.003 | 0.003 | $\mathbf{0 . 0 0 3}$ | 0.003 | 0.004 | 0.441 |
| MAT | $\mathbf{4 3 1 . 7}$ | 408.6 | 459.4 | $\mathbf{3 9 8 . 9}$ | 377.6 | 437.5 | $\mathbf{0 . 0 1 0}$ |

## References:

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